Package 'LGCU'

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itle Implementation of Learning Gamma CUSUM (Cumulative Sum) Control Charts		
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Description Implements Cumulative Sum (CUSUM) control charts specifically designed for monitoring processes following a Gamma distribution. Provides functions to estimate distribution parameters, simulate control limits, and apply cautious learning schemes for adaptive thresholding. It supports upward and downward monitoring with guaranteed performance evaluated via Monte Carlo simulations. It is useful for quality control applications in industries where data follows a Gamma distribution. Methods are based on Madrid-Alvarez et al. (2024) <doi:10.1002 qre.3464=""> and Madrid-Alvarez et al. (2024) <doi:10.1080 08982112.2024.2440368="">.</doi:10.1080></doi:10.1002>		
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Author Harold Manuel Madrid-Alvarez [aut, cre]		
Maintainer Harold Manuel Madrid-Alvarez harold.madrid@unisimon.edu.co>		
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Contents		
ARL_Clminus		

2 ARL_Clminus

ARL_C	lminus ARL Estimation in CUSUM Control Charts with Gamma Distribution and Cautious Learning for downward detection	
Index	3	0
	plot_GICC_chart2	8
	plot_GICCup_chart	
	plot_GICCL_chart2	3
	plot_GICCLup_Chart	1
	plot_GICCLdown_Chart	9
	plot_GICCdown_chart	7
	GICARL_CUSUM_up	6
	GICARL_CUSUM_down	4
	getDeltaH_up	3
	getDeltaH_down	
	getDeltaHL_up	
	getDeltaHL_down	7

Description

This function calculates the **Average Run Length (ARL)** of a CUSUM control chart based on the Gamma distribution, incorporating a cautious learning scheme for the dynamic update of parameters.

The function allows the evaluation of the CUSUM chart's performance under different parameterization scenarios, ensuring efficient detection of process changes.

Based on the methodology presented in the work of Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), this implementation uses Monte Carlo simulations optimized in C++ for efficient execution and progressive adjustment of the control chart parameters.

The values for H_minus, H_delta, K_1, delay, and tau can be referenced in the tables from the article:

Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for the Gamma distribution with cautious parameter learning. Quality Engineering, 1-23.

Usage Scenarios::

Scenario 1: Known alpha and estimated beta

- The alpha parameter is assumed to be fixed and known in advance.
- beta is estimated from a dataset or provided by the user.
- The user must specify alpha and an initial estimate of beta (beta0_est).

Scenario 2: Both alpha and beta are estimated

- Both alpha and beta are estimated from an external dataset.
- The user must calculate alpha0_est and beta0_est before calling the function.
- beta0_est is dynamically updated during the simulation when a predefined condition is met.

Features::

ARL_Clminus 3

- Implements Monte Carlo simulations for ARL estimation.
- Allows dynamic updating of beta0_est to improve model adaptation.
- Uses C++ optimization for efficient and precise execution.
- Compatible with scenarios where alpha is either known or estimated.
- Recommended values for H_minus, H_delta, K_l, delay, and tau can be found in the reference article.

This function is ideal for quality control studies where reliable detection of process changes modeled with Gamma distributions is required.

Usage

```
ARL_Clminus(
  alpha,
 beta,
  alpha0_est,
 beta0_est,
  known_alpha,
 beta_ratio,
 H_delta,
 H_minus,
 n_I,
  replicates,
 K_{1},
 delay,
  tau
)
```

Arguments

alpha	Shape parameter of the Gamma distribution.
beta	Scale parameter of the Gamma distribution.
alpha0_est	Initial estimate of the shape parameter alpha. If known_alpha is TRUE, this value will be equal to alpha.
beta0_est	Initial estimate of the scale parameter beta. This value is updated dynamically during the simulation.
known_alpha	TRUE if alpha@_est is fixed, FALSE if it must be estimated.
beta_ratio	Ratio between beta and its posterior estimate.
H_delta	Increment of the lower control limit in the CUSUM chart.
H_minus	Initial control limit of the CUSUM chart for downward detection.
n_I	Sample size in Phase I.
replicates	Number of Monte Carlo simulations.
K_1	Secondary control threshold for parameter updating.
delay	Number of observations before updating beta@_est.
tau	Time point at which beta changes.

4 ARL_Clplus

Value

A numeric value corresponding to the **ARL** estimate for the downward CUSUM control chart with cautious learning.

Examples

```
# Option 1: Provide parameters directly
ARL_Clminus(
  alpha = 1,
  beta = 1,
  alpha0_est = 1.067, # alpha = known_alpha
  beta0_est = 0.2760,
                        # Estimated Beta
  known_alpha = TRUE,
  beta_ratio = 1/2,
  H_{delta} = 0.6946,
  H_{minus} = -4.8272,
  n_I = 500,
  replicates = 1000,
  K_1 = 0.5,
  delay = 25,
  tau = 1
)
# Option 2: Use generated data
set.seed(123)
datos_faseI <- rgamma(n = 500, shape = 1, scale = 1)</pre>
alpha0_est <- mean(datos_faseI)^2 / var(datos_faseI) # Alpha estimation</pre>
beta0_est <- mean(datos_faseI) / alpha0_est # Beta estimation</pre>
ARL_Clminus(
  alpha = 1,
  beta = 1,
  alpha0_est = 1.067, # alpha = known_alpha
  beta0_est = 0.2760,
                         # Estimated Beta
  known_alpha = FALSE,
  beta_ratio = 1/2,
  H_{delta} = 0.6946,
  H_{minus} = -4.8272,
  n_I = 500,
  replicates = 1000,
  K_1 = 0.5,
  delay = 25,
  tau = 1
)
```

ARL_Clplus

ARL Estimation in CUSUM Control Charts with Gamma Distribution and Cautious Learning for upward detection

ARL_Clplus 5

Description

This function calculates the **Average Run Length** (**ARL**) of a CUSUM control chart based on the Gamma distribution, incorporating a cautious learning scheme for the progressive update of parameters and optimization of performance in upward detection.

The function allows for the evaluation of the CUSUM chart's behavior under different parameterization scenarios, ensuring efficient detection of process changes.

Following the methodology presented in the work of Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), this implementation utilizes Monte Carlo simulations in C++ for efficient execution, ensuring a dynamic adjustment of parameters based on the evolution of the process.

The values of H_plus, H_delta, K_l, delay, and tau can be referenced in the tables from the article:

Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for the Gamma distribution with cautious parameter learning. Quality Engineering, 1-23.

Usage Scenarios::

Scenario 1: Known alpha and estimated beta

- The alpha parameter is assumed to be fixed and known in advance.
- beta is estimated from a dataset or defined by the user.
- The user must provide alpha and an initial estimate of beta (beta@_est).

Scenario 2: Both alpha and beta are estimated

- Both alpha and beta are estimated from a dataset or external data source.
- The user must calculate alpha@_est and beta@_est before running the function.
- beta0_est is dynamically updated during the simulation when a predefined condition is met.

Features::

- Implements Monte Carlo simulations optimized in C++ for ARL estimation.
- Allows dynamic updating of beta0_est to improve the model's adaptability.
- Compatible with scenarios where alpha is known or estimated.
- Ensures stable and reliable performance in detecting changes in processes modeled with Gamma distributions.
- Recommended values for H_plus, H_delta, K_l, delay, and tau can be found in the reference article.

Usage

```
ARL_Clplus(
alpha,
beta,
alpha0_est,
beta0_est,
known_alpha,
beta_ratio,
H_delta,
H_plus,
n_I,
```

6 ARL_Clplus

```
replicates,
K_l,
delay,
tau
)
```

Arguments

alpha Shape parameter of the Gamma distribution. beta Scale parameter of the Gamma distribution. alpha0_est Initial estimate of the shape parameter alpha. If known_alpha is TRUE, this value will be equal to alpha. beta0_est Initial estimate of the scale parameter beta. This value is updated dynamically during the simulation. known_alpha TRUE if alpha0_est is fixed, FALSE if it must be estimated. beta_ratio Ratio between beta and its posterior estimate. Increment of the upper control limit in the CUSUM chart. H_delta Initial control limit of the CUSUM chart. H_plus n_I Sample size in Phase I. Number of Monte Carlo simulations. replicates K_1 Secondary control threshold for parameter updating.

Value

delay

tau

A numeric value corresponding to the **ARL** estimate for the upward CUSUM control chart with cautious learning.

Time point at which beta changes. A value of 1 is recommended for IC states.

Number of observations before updating beta0_est.

```
# Option 1: Provide parameters directly
ARL_Clplus(
 alpha = 1,
 beta = 1,
 alpha0_est = 1, # alpha = known_alpha
 beta0_est = 1.1,  # Estimated Beta
 known_alpha = TRUE,
 beta_ratio = 2,
 H_{delta} = 4.2433,
 H_{plus} = 8.7434,
 n_I = 200,
 replicates = 100,
 K_1 = 2,
 delay = 25,
 tau = 1
)
```

getDeltaHL_down 7

```
# Option 2: Use generated data
set.seed(123)
datos_faseI <- rgamma(n = 200, shape = 1, scale = 1)</pre>
alpha0_est <- mean(datos_faseI)^2 / var(datos_faseI) # Alpha estimation
beta0_est <- mean(datos_faseI) / alpha0_est # Beta estimation</pre>
ARL_Clplus(
 alpha = 1,
 beta = 1,
 alpha0_est = alpha0_est,
 beta0_est = beta0_est,
 known_alpha = FALSE,
 beta_ratio = 2,
 H_{delta} = 4.2433,
 H_{plus} = 8.7434,
 n_I = 200,
 replicates = 1000,
 K_1 = 2,
 delay = 25,
 tau = 1
)
```

getDeltaHL_down

Estimation of the H_delta parameter with learning for downward detection in CUSUM Gamma charts

Description

This function calculates the optimal value of H_delta using a dynamic learning scheme based on the ARL_Clplus function, iteratively adjusting H_delta to achieve an **expected ARL** with greater accuracy and adaptability.

Based on the methodology proposed by Madrid-Alvarez, Garcia-Diaz, and Tercero-Gomez (2024), this function allows adjusting H_delta in different sample size scenarios, ensuring that the control chart progressively adapts to changes in the Gamma distribution.

Features::

- Implements Monte Carlo simulations to estimate H_delta.
- Relies on parameter estimates obtained in Phase I.
- Iteratively adjusts H_delta until the specified ARL is reached.
- Incorporates a cautious learning mechanism to improve adjustment accuracy.
- Displays total execution time using tictoc.

Recommendations:

• This function is useful for estimating H_delta values when the sample size differs from those reported in the reference article:

Madrid-Alvarez, H. M., Garcia-Diaz, J. C., & Tercero-Gomez, V. G. (2024). A CUSUM control chart for the Gamma distribution with cautious parameter learning. Quality Engineering, 1-23.

8 getDeltaHL_down

• The adjustment process is iterative and computationally demanding, as execution time depends on the number of iterations (N_init + N_final) and the sample size (n_I).

- It is recommended to define an appropriate convergence criterion to optimize execution time without compromising accuracy in the estimation of H_delta.
- For selecting values of a, b, k_l, delay, tau, and H_minus, refer to the reference article, which presents specific strategies for their calibration in different scenarios.

Usage

```
getDeltaHL_down(
  n_I,
  alpha,
 beta,
  beta_ratio,
 H_minus,
  a,
  b,
  ARL_esp,
  replicates,
 N_init,
 N_final,
  known_alpha,
 K_1,
  delay,
  tau
)
```

Arguments

n_I	Sample size in Phase I.
alpha	Shape parameter of the Gamma distribution.
beta	Scale parameter of the Gamma distribution.
beta_ratio	Ratio between beta and its posterior estimate.
H_minus	Lower limit of the CUSUM chart.
а	Tolerance level for the expected ARL $(0 \le a \le 1)$.
b	Tolerance level for the expected ARL $(0 < b < 1)$.
ARL_esp	Desired expected ARL value.
replicates	Number of replications in the Monte Carlo simulation.
N_init	Initial iterations for adjustment.
N_final	Final iterations for averaging H_delta.
known_alpha	TRUE if alpha is fixed, FALSE if it must be estimated.
K_1	Secondary control threshold for parameter update.
delay	Number of observations before updating beta@_est.
tau	Time point where beta changes.

getDeltaHL_up 9

Value

A numeric value corresponding to the optimal H_delta estimated with learning for the downward CUSUM control chart.

Examples

getDeltaHL_up

Estimation of the H_delta parameter with learning for upward detection in Gamma CUSUM control charts

Description

This function calculates the optimal value of H_delta using a dynamic learning scheme based on the ARL_Clplus function, iteratively adjusting H_delta to achieve an **expected ARL** with higher accuracy and adaptability.

Based on the methodology proposed by Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), this function allows adjusting H_delta in different sample size scenarios, ensuring that the control chart progressively adapts to changes in the Gamma distribution.

Features::

- Implements Monte Carlo simulations to estimate H_delta.
- Relies on parameter estimates obtained in Phase I.
- Iteratively adjusts H_delta until the specified ARL is reached.
- Incorporates a cautious learning mechanism to improve adjustment precision.
- Displays the total execution time using tictoc.

Recommendations:

- This function is useful for estimating H_delta values when the sample size differs from the values reported in the reference article:
 - Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for the Gamma distribution with cautious parameter learning. Quality Engineering, 1-23.
- The adjustment process is iterative and computationally intensive, as execution time depends on the number of iterations (N_init + N_final) and the sample size (n_I).
- It is recommended to define a proper convergence criterion to optimize execution time without compromising the accuracy of H_delta estimation.
- For selecting values of a, b, k_1, delay, tau, and H_plus, consulting the reference article is recommended, as it provides specific strategies for their calibration in different scenarios.

10 getDeltaHL_up

Usage

```
getDeltaHL_up(
  n_I,
  alpha,
 beta,
 beta_ratio,
 H_plus,
  a,
 b,
 ARL_esp,
 replicates,
 N_init,
 N_final,
 known_alpha,
 K_{1},
 delay,
  tau
)
```

Arguments

n_I	Sample size in Phase I.
alpha	Shape parameter of the Gamma distribution.
beta	Scale parameter of the Gamma distribution.
beta_ratio	Ratio between beta and its posterior estimate.
H_plus	Initial limit of the CUSUM chart.
а	Tolerance level for the expected ARL. $(0 \le a \le 1)$.
b	Tolerance level for the expected ARL. $(0 < b < 1)$
ARL_esp	Desired expected ARL value.
replicates	Number of replications in the Monte Carlo simulation.
N_init	Number of initial iterations for adjustment.
N_final	Number of final iterations for averaging H_delta.
known_alpha	TRUE if alpha is fixed, FALSE if it should be estimated.
K_1	Secondary control threshold for parameter updating.
delay	Number of observations before updating beta@_est.
tau	Point in time where beta changes.

Value

A numeric value corresponding to the optimal H_delta estimated with learning for the upward CUSUM control chart.

getDeltaH_down 11

Examples

getDeltaH_down

Estimation of the Optimal H_delta Value to Guarantee Performance in the Downward CUSUM Control Chart

Description

This function calculates the optimal value of H_delta that guarantees a specific performance in the Gamma CUSUM control chart for downward detection. It employs a Monte Carlo simulation approach and an iterative adjustment process to determine the appropriate value.

Following the methodology presented by Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), this function allows adjusting H_delta for different sample size configurations, ensuring that the control chart maintains the desired performance in terms of expected ARL.

Features::

- Implements Monte Carlo simulations to estimate H_delta.
- Based on parameter estimates obtained in Phase I.
- Iteratively adjusts H_delta until the specified ARL is achieved.
- Displays the total execution time using tictoc.

Recommendations:

- This function is useful for estimating H_delta values in scenarios where the sample size differs from the values reported in the reference paper:
 - Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for gamma distribution with guaranteed performance. Quality and Reliability Engineering International, 40(3), 1279-1301.
- The adjustment process is iterative and computationally demanding, as its execution time depends on the number of iterations (N_init + N_final) and the sample size (n_I).
- It is recommended to establish an appropriate convergence criterion to optimize execution time without compromising the accuracy of H_delta estimation.
- For selecting values of H_minus, a, and b, it is advisable to consult the reference paper, which provides specific calibration strategies and recommendations.

12 getDeltaH_down

Usage

```
getDeltaH_down(
    n_I,
    alpha,
    beta,
    beta_ratio,
    H_minus,
    a,
    b,
    ARL_esp,
    m,
    N_init,
    N_final,
    known_alpha
)
```

Arguments

n_I	Sample size in Phase I.
alpha	Shape parameter of the Gamma distribution.
beta	Scale parameter of the Gamma distribution.
beta_ratio	Ratio between beta and its estimate.
H_minus	Initial lower limit of the CUSUM chart.
a	Tolerance level for the expected ARL $(0 \le a \le 1)$.
b	Tolerance level for the expected ARL $(0 < b < 1)$.
ARL_esp	Desired expected ARL value.
m	Number of states in the Markov matrix.
N_init	Number of initial iterations.
N_final	Number of final iterations.
known_alpha	Indicates whether alpha is known (TRUE) or should be estimated (FALSE).

Value

A numerical value corresponding to the optimal H_delta for the downward CUSUM control chart, ensuring the expected performance.

getDeltaH_up 13

getDeltaH_up	Estimation of the optimal H_delta value to guarantee performance in the upward CUSUM control chart

Description

This function calculates the optimal H_delta value that ensures specific performance in the Gamma CUSUM control chart for upward detection. It relies on Monte Carlo simulations and an iterative adjustment process to determine the appropriate value.

Following the methodology proposed by Madrid-Alvarez, Garcia-Diaz, and Tercero-Gomez (2024), this function allows adjusting H_delta for different sample size scenarios, ensuring that the control chart maintains the expected performance in terms of ARL.

Features::

- Implements Monte Carlo simulations to estimate H_delta.
- Based on parameter estimates obtained in Phase I.
- Iteratively adjusts H_delta until the specified ARL is reached.
- Displays total execution time using tictoc.

Recommendations:

- This function is useful for estimating H_delta values in scenarios where the sample size differs from the values reported in the reference article:
 - Madrid-Alvarez, H. M., Garcia-Diaz, J. C., & Tercero-Gomez, V. G. (2024). A CUSUM control chart for gamma distribution with guaranteed performance. Quality and Reliability Engineering International, 40(3), 1279-1301.
- The adjustment process is iterative and computationally demanding, as its execution time depends on the number of iterations (N_init + N_final) and the sample size (n_I).
- It is recommended to establish an appropriate convergence criterion to optimize execution time without compromising the accuracy of H_delta estimation.
- For selecting values of H_plus, a, and b, refer to the reference article, which presents specific strategies and recommendations for calibration.

Usage

```
getDeltaH_up(
    n_I,
    alpha,
    beta,
    beta_ratio,
    H_plus,
    a,
    b,
    ARL_esp,
    m,
    N_init,
```

```
N_final,
  known_alpha
)
```

Arguments

n_I	Sample size in Phase I.
alpha	Shape parameter of the Gamma distribution.
beta	Scale parameter of the Gamma distribution.
beta_ratio	Ratio between beta and its estimate.
H_plus	Initial upper limit of the CUSUM chart.
а	Tolerance level for the expected ARL $(0 \le a \le 1)$.
b	Tolerance level for the expected ARL $(0 < b < 1)$.
ARL_esp	Desired expected ARL value.
m	Number of states in the Markov matrix.
N_init	Number of initial iterations.
N_final	Number of final iterations.

Value

known_alpha

A numeric value corresponding to the optimal H_delta for the upward CUSUM control chart, ensuring the expected performance.

Indicates whether alpha is known (TRUE) or needs to be estimated (FALSE).

Examples

GICARL_CUSUM_down

ARL Calculation for a Downward CUSUM Control Chart with a Gamma Distribution

Description

This function estimates the average run length (ARL) of a downward CUSUM control chart applied to a Gamma distribution with guaranteed performance (GIC), considering both known and estimated parameters.

This approach follows the methodology described in the work of Madrid-Alvarez, García-díaz, and Tercero-Gómez(2024), which provides a detailed analysis of the performance of CUSUM control charts for Gamma distributions with guaranteed efficiency. Specifically, the method implemented in this function enables the precise evaluation of ARL under different parameter settings, ensuring appropriate calibration and monitoring of controlled processes.

Recommendations:

For further consultation and to review values of H_delta and H_minus, it is recommended to refer to the following article: Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for gamma distribution with guaranteed performance. Quality and Reliability Engineering.

Considerations::

- The control chart is calibrated with beta = 1.
- When alpha and beta are known, it is recommended to use the same values for alpha_est = alpha and beta_est = 1.
- Higher values of m increase the accuracy of the results (m = {10, 100}).

Usage

```
GICARL_CUSUM_down(
   alpha,
   beta,
   alpha_est,
   beta_est,
   beta_ratio,
   H_minus,
   H_delta,
   m
)
```

Arguments

alpha Shape parameter of the Gamma distribution. Scale parameter of the Gamma distribution. beta alpha_est Estimated shape parameter. beta_est Estimated scale parameter. beta_ratio Ratio between beta and its estimation. Lower control limit of the downward CUSUM chart. H_minus H_delta Increment of the GIC threshold. m Number of divisions for the probability matrix.

Value

A numeric value representing the average run length (ARL) of the downward CUSUM control chart.

GICARL_CUSUM_up

ARL Calculation for an Upward CUSUM Control Chart with a Gamma Distribution

Description

This function estimates the average run length (ARL) of an upward CUSUM control chart applied to a Gamma distribution with guaranteed performance (GIC), considering both known and estimated parameters.

This approach follows the methodology described in the work of Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), which provides a detailed analysis of the performance of CUSUM control charts for Gamma distributions with guaranteed efficiency. Specifically, the method implemented in this function enables the precise evaluation of ARL under different parameter settings, ensuring appropriate calibration and monitoring of controlled processes.

Recommendations:

For further consultation and to review values of H_delta and H_plus, it is recommended to refer to the following article: Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for gamma distribution with guaranteed performance. Quality and Reliability Engineering.

Key Considerations::

- The control chart is calibrated with beta = 1.
- When alpha and beta are known, it is recommended to use the same values for alpha_est = alpha and beta_est = 1.
- Higher values of m increase the accuracy of the results ($m = \{10, 100\}$).

Usage

```
GICARL_CUSUM_up(
   alpha,
   beta,
   alpha_est,
   beta_est,
   beta_ratio,
   H_plus,
   H_delta,
   m
)
```

plot_GICCdown_chart

17

Arguments

alpha	Shape parameter of the Gamma distribution.
beta	Scale parameter of the Gamma distribution.

alpha_est Estimated shape parameter. beta_est Estimated scale parameter.

beta_ratio Ratio between beta and its estimation.

H_plus Upper control limit of the upward CUSUM chart.

H_delta Increment of the GIC threshold.

m Number of divisions for the probability matrix.

Value

A numeric value representing the average run length (ARL) of the upward CUSUM control chart.

Examples

Description

This function generates a downward CUSUM control chart for a Gamma distribution, displaying the evolution of the CUSUM statistic, control limits, and a summary of the parameters.

Based on the approach presented by Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), this implementation allows for the evaluation and visualization of monitored processes using a CUSUM chart adapted to Gamma distributions with guaranteed performance.

In particular, the function incorporates a Monte Carlo model to simulate the behavior of the control chart, allowing for the estimation of the Gamma distribution in Phase I or the use of predefined values. Additionally, it provides a clear graphical representation of the evolution of the CUSUM statistic, ensuring appropriate calibration and process control.

Recommendations:

To reference specific values of H_delta and H_minus, it is recommended to consult the following article: Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for gamma distribution with guaranteed performance. Quality and Reliability Engineering International, 40(3), 1279-1301.

Features::

- Based on a Monte Carlo model.
- The Gamma distribution is either estimated in Phase I or predefined values are used.
- Accumulated values of the CUSUM statistic with guaranteed performance are plotted.
- Control limits and a summary table are included.

Usage

```
plot_GICCdown_chart(
   alpha,
   beta,
   beta_ratio,
   H_delta,
   H_minus,
   n_I,
   n_II,
   faseI = NULL,
   faseII = NULL,
   known_alpha
)
```

Arguments

alpha	Shape parameter of the Gamma distribution.
beta	Scale parameter of the Gamma distribution.
beta_ratio	Ratio between beta and its estimation.
H_delta	Increment of the lower control limit (GIC).
H_minus	Initial lower control limit of the CUSUM chart.
n_I	Sample size in Phase I (if faseI is not provided).
n_II	Sample size in Phase II (if faseII is not provided).
faseI	Data sample from Phase I (numeric vector). If NULL, it is generated using $rgamma()$.
faseII	Data sample from Phase II (numeric vector). If NULL, it is generated using rgamma().
known_alpha	If TRUE, a known alpha is used; if FALSE, it is estimated.

Value

A plot showing the evolution of the downward CUSUM statistic, including:

- The accumulated values of the CUSUM statistic.
- Control limits with guaranteed performance.
- A summary of the parameters used in the control chart.

Examples

Description

This function generates a downward CUSUM control chart for a Gamma distribution, incorporating a cautious parameter updating mechanism based on guaranteed performance.

It enables dynamic process monitoring, ensuring progressive adaptation to changes in the distribution.

This approach follows the methodology presented in the work of Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), where a cautious learning scheme for parameter updating in CUSUM control charts applied to Gamma distributions is proposed.

The implementation captures changes in the distribution and adjusts the control limits to enhance the detection of process variations.

Features::

- If the user does not provide Phase I and Phase II data, the function generates them automatically.
- If known_alpha = TRUE, alpha is fixed and not estimated.
- If known_alpha = FALSE, alpha is estimated from Phase I data.
- Dynamic control limits and a summary of parameters are included.
- Integrates a cautious learning scheme using the parameters k_1, delay, and tau.

Recommendations:

The parameters k_1, delay, and tau are part of the cautious learning mechanism of the CUSUM chart. These values enable the dynamic updating of beta0_est and H_minus, ensuring that the

control chart progressively adapts to process changes, improving sensitivity in detecting deviations.

For proper implementation, it is recommended to reference the values proposed in:

Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for the Gamma distribution with cautious parameter learning. Quality Engineering, 1-23.

While these parameters have been tested and validated in the referenced article, users can adjust them based on the specific characteristics of their process, considering factors such as system variability and desired update frequency.

Additionally, if detailed guidance on selecting values for H_delta and H_minus is needed, it is recommended to review the referenced article, which presents calibration and adjustment strategies for these limits to ensure optimal control chart performance.

Usage

```
plot_GICCLdown_Chart(
   alpha,
   beta,
   beta_ratio,
   H_delta,
   H_minus,
   known_alpha,
   k_l,
   delay,
   tau,
   n_I,
   n_II,
   faseI = NULL,
   faseII = NULL
)
```

Arguments

alpha	Shape parameter of the Gamma distribution (if alpha_conocido = TRUE).
beta	Scale parameter of the Gamma distribution.
beta_ratio	Ratio between beta and its estimation.
H_delta	Increment of the lower control limit.
H_minus	Initial lower control limit of the CUSUM chart.
known_alpha	Indicates whether alpha is known (TRUE) or should be estimated (FALSE).
k_1	Secondary control threshold used in the learning logic.
delay	Number of observations before updating beta0_est and H_minus_c.
tau	Time point at which the beta parameter changes.
n_I	Sample size in Phase I (if faseI is not provided).
n_II	Sample size in Phase II (if faseII is not provided).
faseI	Data sample from Phase I (numeric vector). If NULL, it is generated internally.
faseII	Data sample from Phase II (numeric vector). If NULL, it is generated internally.

plot_GICCLup_Chart

Value

A plot showing the evolution of the downward CUSUM statistic with cautious learning, including:

21

- The dynamically adjusted accumulated values of the CUSUM statistic.
- Progressively updated control limits with guaranteed performance.
- A summary of the parameters used in the control chart.

Examples

plot_GICCLup_Chart

Upward CUSUM Control Chart with Cautious Learning and Guaranteed Performance

Description

This function generates an upward CUSUM control chart for a Gamma distribution, incorporating a cautious parameter update mechanism based on guaranteed performance.

It enables dynamic process monitoring, ensuring progressive adaptation to distribution changes. This approach follows the methodology presented in the work of Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), where a cautious learning scheme for parameter updates in CUSUM control charts applied to Gamma distributions is proposed.

The implementation captures distribution changes and adjusts the control limits to improve process variation detection.

Features::

- If the user does not provide Phase I and Phase II data, the function automatically generates
- If known_alpha = TRUE, alpha is fixed and not estimated.
- If known_alpha = FALSE, alpha is estimated from Phase I data.

- Includes dynamic control limits and a summary of parameters.
- Integrates a cautious learning scheme using the parameters k_1, delay, and tau.

Recommendations:

The parameters k_1, delay, and tau are part of the cautious learning mechanism of the CUSUM chart. These values enable the dynamic updating of beta@_est and H_plus, ensuring that the control chart progressively adapts to process changes, thus improving sensitivity in detecting deviations.

For proper implementation, it is recommended to reference the values proposed in:

Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for the Gamma distribution with cautious parameter learning. Quality Engineering, 1-23.

While these parameters have been tested and validated in the referenced article, users can adjust them based on the specific characteristics of their process, considering factors such as system variability and desired update frequency.

Additionally, if detailed guidance on selecting values for H_delta and H_plus is required, it is recommended to review the referenced article, which presents calibration and adjustment strategies for these limits to ensure optimal control chart performance.

Usage

```
plot_GICCLup_Chart(
   alpha,
   beta,
   beta_ratio,
   H_delta,
   H_plus,
   known_alpha,
   k_l,
   delay,
   tau,
   n_I,
   n_II,
   faseI = NULL,
   faseII = NULL
)
```

Arguments

alpha Shape parameter of the Gamma distribution (if known_alpha = TRUE).

beta Scale parameter of the Gamma distribution.

beta_ratio Ratio between beta and its estimation.

H_delta Increment of the upper control limit.

H_plus Initial upper control limit of the CUSUM chart.

known_alpha Indicates whether alpha is known (TRUE) or should be estimated (FALSE).

Secondary control threshold used in the learning logic.

plot_GICCL_chart2 23

delay	Number of observations before updating beta0_est and H_plus_c.
tau	Time point at which the beta parameter changes.
n_I	Sample size in Phase I (if faseI is not provided).
n_II	Sample size in Phase II (if faseII is not provided).
faseI	Data sample from Phase I (numeric vector). If NULL, it is generated internally.
faseII	Data sample from Phase II (numeric vector). If NULL, it is generated internally.

Value

A plot showing the evolution of the upward CUSUM statistic with cautious learning, including:

- The dynamically adjusted accumulated values of the CUSUM statistic.
- Progressively updated control limits with guaranteed performance.
- A summary of the parameters used in the control chart.

Examples

plot_GICCL_chart2

CUSUM Control Chart with Cautious Learning and Guaranteed Performance

Description

This function generates a bidirectional (upward and downward) CUSUM control chart for a Gamma distribution, incorporating a cautious parameter update mechanism with guaranteed performance. Its purpose is to enhance sensitivity and precision in detecting changes in dynamic processes.

Based on the methodology presented by Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), this implementation allows control limits to adapt according to the evolution of the process, ensuring early detection of variations while minimizing the risk of false alarms.

Features::

24 plot_GICCL_chart2

• If the user does not provide Phase I and Phase II data, the function automatically generates them.

- If known_alpha = TRUE, alpha is fixed and not estimated.
- If known_alpha = FALSE, alpha is estimated from Phase I data.
- Includes dynamic control limits and a summary table of parameters.
- Enables the detection of both upward and downward deviations, progressively adjusting the control limits.

Recommendations:

- The parameters k_1, delay, and tau are crucial for the learning process in the control chart. They regulate the progressive update of control limits, allowing the dynamic update of beta0_est, H_plus_c, and H_minus_c, ensuring that the control chart gradually adjusts to changes in the process. It is recommended to use reference values presented in:
 - Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for the Gamma distribution with cautious parameter learning. Quality Engineering, 1-23.
- Similar to the parameters above, for proper selection of H_plus, H_minus, H_delta_plus, and H_delta_minus values, it is recommended to review the reference article, where detailed calibration strategies for different scenarios are presented.

Usage

```
plot_GICCL_chart2(
  alpha,
  beta,
  beta_ratio_plus,
  beta_ratio_minus,
 H_delta_plus,
 H_plus,
 H_delta_minus,
 H_minus,
  known_alpha,
  k_{1},
  delay,
  tau,
  n_I,
 n_II,
  faseI = NULL,
  faseII = NULL
)
```

Arguments

alpha Shape parameter of the Gamma distribution (if known_alpha = TRUE).

beta Scale parameter of the Gamma distribution.

beta_ratio_plus

Ratio between beta and its estimate for upward detection.

plot_GICCL_chart2 25

beta_ratio_minus

Ratio between beta and its estimate for downward detection.

H_delta_plus Increment of the upper control limit.
H_plus Initial upper limit of the CUSUM chart.
H_delta_minus Increment of the lower control limit.
H_minus Initial lower limit of the CUSUM chart.

known_alpha Indicates whether alpha is known (TRUE) or should be estimated (FALSE).

k_1 Secondary control threshold used in the learning logic.

delay Number of observations before updating beta@_est, H_plus_c, and H_minus_c.

tau Time point at which the beta parameter changes.

n_I Sample size in Phase I (if faseI is not provided).

n_II Sample size in Phase II (if faseII is not provided).

faseI Data sample from Phase I (numeric vector). If NULL, it is generated internally.

Data sample from Phase II (numeric vector). If NULL, it is generated internally.

Value

A plot showing the evolution of the CUSUM statistic with cautious learning, including:

- Dynamically adjusted accumulated values of the CUSUM statistic.
- Progressively updated control limits with guaranteed performance.
- A summary of the parameters used in the control chart.

```
# Option 1: Automatically generated data
plot_GICCL_chart2(alpha = 1, beta = 1,
                 beta_ratio_plus = 2, beta_ratio_minus = 0.5,
                 H_delta_plus = 3.0, H_plus = 6.5,
                 H_delta_minus = 2.0, H_minus = -5.0,
                 known_alpha = TRUE, k_1 = 2, delay = 25, tau = 1,
                 n_I = 200, n_{II} = 700,
                 faseI = NULL, faseII = NULL)
# Option 2: User-provided data
datos_faseI <- rgamma(n = 200, shape = 1, scale = 1)</pre>
datos_faseII <- rgamma(n = 700, shape = 1, scale = 1)</pre>
plot_GICCL_chart2(alpha = 1, beta = 1,
                 beta_ratio_plus = 2, beta_ratio_minus = 0.5,
                 H_delta_plus = 3.0, H_plus = 6.5,
                 H_delta_minus = 2.0, H_minus = -5.0,
                 known_alpha = FALSE, k_l = 2, delay = 25, tau = 1,
                 n_I = 200, n_I = 700,
                 faseI = datos_faseI, faseII = datos_faseII)
```

26 plot_GICCup_chart

plot_GICCup_chart

Upward CUSUM Control Chart for Gamma Distribution with Guaranteed Performance

Description

This function generates an upward CUSUM control chart for a Gamma distribution, displaying the evolution of the CUSUM statistic, control limits, and a summary of the parameters.

Based on the approach presented by Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), this implementation enables the evaluation and visualization of the monitored process using a CUSUM chart adapted to Gamma distributions with guaranteed performance.

Specifically, the library incorporates a Monte Carlo model for simulating the control chart behavior, allowing the Gamma distribution to be estimated in Phase I or using predefined values. Additionally, it provides a clear graphical representation of the CUSUM statistic's evolution, ensuring proper calibration and process control.

Recommendations:

To check specific values for H_delta and H_plus, it is recommended to review the reference article: Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for gamma distribution with guaranteed performance. Quality and Reliability Engineering International, 40(3), 1279-1301.

Features::

- · Based on a Monte Carlo model.
- Estimates the Gamma distribution in Phase I or uses predefined values.
- Plots the accumulated values of the CUSUM statistic with guaranteed performance.
- Includes control limits and a summary table.

Usage

```
plot_GICCup_chart(
   alpha,
   beta,
   beta_ratio,
   H_delta,
   H_plus,
   n_I,
   n_II,
   faseI = NULL,
   faseII = NULL,
   known_alpha
)
```

plot_GICCup_chart 27

Arguments

alpha	Shape parameter of the Gamma distribution.
beta	Scale parameter of the Gamma distribution.
beta_ratio	Ratio between beta and its estimation.
H_delta	Increment of the upper GIC limit.
H_plus	Initial upper limit of the CUSUM chart.
n_I	Sample size in Phase I (if faseI is not provided).
n_II	Sample size in Phase II (if faseII is not provided).
faseI	Sample data from Phase I (numeric vector). If NULL, it is generated with rgamma().
faseII	Sample data from Phase II (numeric vector). If NULL, it is generated with rgamma().
known_alpha	If TRUE, a known alpha is used; if FALSE, it is estimated.

Value

A plot displaying the evolution of the upward CUSUM statistic, including:

- The accumulated values of the CUSUM statistic.
- Control limits with guaranteed performance.
- A summary of the parameters used in the control chart.

28 plot_GICC_chart2

plot_GICC_chart2

CUSUM Control Chart for Gamma Distribution with Guaranteed Performance

Description

This function generates a bidirectional (upward and downward) CUSUM control chart for a Gamma distribution, allowing the monitoring of the evolution of the CUSUM statistic while ensuring optimal performance in detecting process changes.

Based on the methodology proposed by Madrid-Alvarez, García-Díaz, and Tercero-Gómez (2024), this implementation employs a Monte Carlo-based approach to estimate the Gamma distribution parameters and determine control limits with precise calibration. The function enables visualization of process evolution and the detection of deviations with reduced risk of false alarms.

Features::

- Implements Monte Carlo simulations for control chart calibration.
- Allows the use of known Gamma distribution values or estimation in Phase I.
- Provides a graphical representation of the CUSUM statistic evolution with guaranteed performance.
- Includes control limits and a legend with key configuration details of the control chart.

For additional details on selecting parameters H_plus, H_minus, H_delta_plus, and H_delta_minus, as well as calibration strategies, it is recommended to consult the reference article:

Madrid-Alvarez, H. M., García-Díaz, J. C., & Tercero-Gómez, V. G. (2024). A CUSUM control chart for gamma distribution with guaranteed performance. Quality and Reliability Engineering International, 40(3), 1279-1301.

Usage

```
plot_GICC_chart2(
    alpha,
    beta,
    beta_ratio_plus,
    beta_ratio_minus,
    H_delta_plus,
    H_plus,
    H_delta_minus,
    H_minus,
    n_I,
    n_II,
    faseI = NULL,
    known_alpha
)
```

plot_GICC_chart2 29

Arguments

alpha Shape parameter of the Gamma distribution.
beta Scale parameter of the Gamma distribution.

beta_ratio_plus

Ratio between beta and its estimation for upward detection.

beta_ratio_minus

Ratio between beta and its estimation for downward detection.

H_delta_plus Increment of the upper GIC limit.
H_plus Initial upper limit of the CUSUM chart.
H_delta_minus Increment of the lower GIC limit.
H_minus Initial lower limit of the CUSUM chart.

n_I Sample size in Phase I (if faseI is not provided).n_II Sample size in Phase II (if faseII is not provided).

faseI Sample data from Phase I (numeric vector). If NULL, it is generated with rgamma().

Sample data from Phase II (numeric vector). If NULL, it is generated with

rgamma().

known_alpha If TRUE, a known alpha is used; if FALSE, it is estimated.

Value

A plot showing the evolution of the CUSUM statistic for a Gamma distribution with guaranteed performance, including:

- The accumulated values of the CUSUM statistic.
- Control limits with guaranteed performance.
- A summary of the parameters used in the control chart.

Index

```
ARL_Clminus, 2
ARL_Clplus, 4

getDeltaH_down, 11
getDeltaH_up, 13
getDeltaHL_down, 7
getDeltaHL_up, 9
GICARL_CUSUM_down, 14
GICARL_CUSUM_up, 16

plot_GICC_chart2, 28
plot_GICCLdown_chart, 17
plot_GICCL_chart2, 23
plot_GICCLdown_Chart, 19
plot_GICCLup_Chart, 21
plot_GICCup_chart, 26
```