

Package ‘simplifyNet’

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Type Package

Title Network Sparsification

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Maintainer Alexander Mercier <amercier@g.harvard.edu>

Description Network sparsification with a variety of novel and known network sparsification techniques. All network sparsification techniques reduce the number of edges, not the number of nodes. Network sparsification is sometimes referred to as network dimensionality reduction. This package is based on the work of Spielman, D., Srivastava, N. (2009)<[arXiv:0803.0929](#)>. Koutis I., Levin, A., Peng, R. (2013)<[arXiv:1209.5821](#)>. Toivonen, H., Mahler, S., Zhou, F. (2010)<[doi:10.1007](#)>. Foti, N., Hughes, J., Rockmore, D. (2011)<[doi:10.1371](#)>.

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Author Andrew Kramer [aut],
Alexander Mercier [aut, cre, trl],
Shubhankar Tripathi [ctb],
Tomlin Pulliam [ctb],
John Drake [ctb] (<<https://orcid.org/0000-0003-4646-1235>>)

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R topics documented:

bestpath	2
EffR	3
EffRSparse	4

EList_Mtrx	6
gns	6
irefit	7
lans	8
Mtrx_EList	10
net.as	10

Index	12
--------------	-----------

bestpath	<i>Sparsification via Best Path</i>
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Description

Calculates network sparsifier from best path

Usage

```
bestpath(network, directed = FALSE, associative = TRUE)
```

Arguments

network	Weighted adjacency matrix, weighted igraph network, or edge list formatted n1 n2 weight with colnames c("n1", "n2", "weight").
directed	If TRUE, specifies that the inputted network is directed. Default is FALSE.
associative	Designates if the network is associative where edge weight determines "similarity" or "strength" or dissociative where edge weight denotes "dissimilarity" or "distance". If the network is associative, then the shortest path would be found by looking at w_e^{-1} where weaker association between nodes suggests a larger distance between nodes for shortest paths. If the network is dissociative, then the shortest path would be between w_e .

Value

Edge list of sparsified network via best path.

Author(s)

Alexander Mercier
Andrew Kramer

References

Toivonen, H., Mahler, S., & Zhou, F. (2010, May). A framework for path-oriented network simplification. In *International Symposium on Intelligent Data Analysis* (pp. 220-231). Springer, Berlin, Heidelberg.

Examples

```
#Generate random ER graph with uniformly random edge weights
g = igraph::erdos.renyi.game(50, 0.1)
igraph::E(g)$weight <- runif(length(igraph::E(g)))
#Sparsify g via bestpath
S = simplifyNet::bestpath(g, directed = FALSE, associative = TRUE) #Show edge list conversion
sg = simplifyNet::net.as(S, net.to="igraph", directed=FALSE)
igraph::ecount(sg)/igraph::ecount(g)#fraction of edges in the sparsifier
```

 EffR

Effective resistances calculator

Description

Calculate or approximate the effective resistances of an inputted, undirected graph. There are three methods.

- (1) 'ext' which exactly calculates the effective resistances (WARNING! Not ideal for large graphs).
- (2) 'spl' which approximates the effective resistances of the inputted graph using the original Spielman-Srivastava algorithm.
- (3) 'kts' which approximates the effective resistances of the inputted graph using the implementation by Koutis et al. (ideal for large graphs where memory usage is a concern).

The relative fidelity of the approximation methods is governed by the variable epsilon.

Usage

```
EffR(network, epsilon = 0.1, type = "kts", tol = 1e-10)
```

Arguments

network	Weighted adjacency matrix, weighted igraph network, or edge list formatted n1 n2 weight with colnames c("n1", "n2", "weight").
epsilon	Variable epsilon governs the relative fidelity of the approximation methods 'spl' and 'kts'. The smaller the value the greater the fidelity of the approximation. Default value is 0.1.
type	There are three methods. (1) 'ext' which exactly calculates the effective resistances (WARNING! Not ideal for large graphs). (2) 'spl' which approximates the effective resistances of the inputted graph using the original Spielman-Srivastava algorithm. (3) 'kts' which approximates the effective resistances of the inputted graph using the implementation by Koutis et al. (ideal for large graphs where memory usage is a concern).
tol	Tolerance for the linear algebra (conjugate gradient) solver to find the effective resistances. Default value is 1e-10.

Details

The fidelity of the effective resistance approximation decreases with a decrease in epsilon. However, it is more important for sparsification by effective resistances that the approximations be roughly equivalent relative to one another, as they will be normalized in a probability distribution where exact values are not needed.

The number of edges contained in the sparsifier will be less than or equal to the number of samples taken, q .

Value

Return either exact or approximate effective resistances for each edge in the same order as "weight" in the edge list.

Author(s)

Alexander Mercier

References

Spielman, D. A., & Srivastava, N. (2011). Graph sparsification by effective resistances. *SIAM Journal on Computing*, 40(6), 1913-1926.

Koutis, I., Miller, G. L., & Peng, R. (2014). Approaching optimality for solving SDD linear systems. *SIAM Journal on Computing*, 43(1), 337-354.

Examples

```
E_List = matrix(c(1,1,2,2,3,3,1,1,1), 3, 3) #Triangle graph, \eqn{K_3}, with edge weights equal to 1
effR = simplifyNet::EffR(E_List, epsilon = 0.1, type = 'kts', tol = 1e-10)
```

EffR Sparse

Sparsification through edge sampling via effective resistances

Description

Sparsify an undirected network by sampling edges proportional to $w_e * R_e$ where w_e is the weight of edge e and R_e is the effective resistance of edge e .

Approximately preserves the graph Laplacian, L , with increasing fidelity as the number of samples taken increases.

Usage

```
EffR Sparse(network, q, effR, seed, n)
```

Arguments

network	Weighted adjacency matrix, weighted igraph network, or edge list formatted n1 n2 weight with colnames c("n1", "n2", "weight").
q	The numbers of samples taken. The fidelity to the original network increases as the number of samples increases, but decreases the sparseness.
effR	Effective resistances corresponding to each edge. Should be in the same order as "weight".
seed	Set the seed to reproduce results of random sampling.
n	The number of nodes in the network. Default is the max node index of the edge list.

Details

The performance of this method is dependent on the size of the network and fidelity of the effective resistance approximation. The network should be "sufficiently large."

For more details, see: <https://epubs.siam.org/doi/epdf/10.1137/080734029>

Value

A sparsified network, H, edge list where the number of edges is dependent on the number of samples taken, q.

Author(s)

Daniel A. Spielman,
Alexander Mercier

References

Spielman, D. A., & Srivastava, N. (2011). Graph sparsification by effective resistances. *SIAM Journal on Computing*, 40(6), 1913-1926.

Examples

```
#Generate random ER graph with uniformly random edge weights
g = igraph::erdos.renyi.game(100, 0.1)
igraph::E(g)$weight <- runif(length(igraph::E(g)))
#Approximate effective resistances
effR = simplifyNet::EffR(g)
#Use effective resistances to create spectral sparsifier by edge sampling
S = simplifyNet::EffRSparse(g, q = 200, effR = effR, seed = 150)
sg = simplifyNet::net.as(S, net.to="igraph", directed=FALSE)
igraph::ecount(sg)/igraph::ecount(g)#fraction of edges in the sparsifier
```

EList_Mtrx	<i>Edge list to adjacency matrix</i>
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Description

Convert an edge list to an adjacency matrix.

Usage

```
EList_Mtrx(E_List, directed = FALSE, n)
```

Arguments

E_List	Edge list formatted n1 n2 weight .
directed	Specifies if the network is directed or undirected. Default is set to undirected.
n	Specify number of nodes. Default is $\max(\text{E_List}[, 1:2])$.

Value

Adjacency matrix constructed from edge list, E_List, of the class dgCMatrix.

Author(s)

Alexander Mercier

gns	<i>Global Network Sparsification</i>
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Description

Remove all edges under certain edge weight threshold.

Usage

```
gns(network, remove.prop, cutoff, directed = FALSE)
```

Arguments

network	Weighted adjacency matrix, weighted igraph network, or edge list formatted n1 n2 weight with colnames c("n1", "n2", "weight").
remove.prop	The proportion of highest weighted edges to retain. A value between 0 and 1.
cutoff	Threshold value for edge weight thresholding.
directed	If TRUE, specifies that the inputted network is directed. Default is FALSE.

Value

Edge list of sparsified network

Author(s)

Andrew Kramer
Alexander Mercier

Examples

```
#Generate random ER graph with uniformly random edge weights
g = igraph::erdos.renyi.game(100, 0.1)
igraph::E(g)$weight <- runif(length(igraph::E(g)))
#Sparsify g via GNS
S = gns(g, remove.prop = 0.5)
sg = simplifyNet::net.as(S, net.to="igraph", directed=FALSE)
igraph::ecount(sg)/igraph::ecount(g)#fraction of edges in the sparsifier
```

 irefit

Iterative refitting

Description

Iterative sparsification based refitting.

Usage

```
irefit(
  network,
  func,
  tol,
  rank = "none",
  connected = FALSE,
  directed = FALSE,
  per = 0.5
)
```

Arguments

network	Weighted adjacency matrix, weighted igraph network, or edge list formatted n1 n2 weight with colnames c("n1", "n2", "weight").
func	Model function whose input is the network and whose output is a single real value or a list of reevaluated weights in the first index and a real value in the second. A wrapper function may have to be written.
tol	Allowed error around the original output of func approximated by the sparsified network within which edges are removed. Specifies if method converges.

rank	Ranking of edges. Lower ranked edges are removed first. Must be the same length as nrow(E_List).
connected	If TRUE, connectivity of the network is prioritized over scoring by func.
directed	If TRUE, specifies that the inputted network is directed. Default is FALSE.
per	Percentage of edges to add/remove from the sparsifier at each step.

Value

Sparsified network, H, which still maintains evaluator function, func, plus/minus tol.

Author(s)

Alexander Mercier

Andrew Kramer

Examples

```
#Set scoring function
mean.weight.degree <- function(graph){
  graph.ob <- igraph::graph_from_edgelist(graph[,1:2])
  igraph::E(graph.ob)$weight <- graph[,3]
  return(mean(igraph::strength(graph.ob)))
}

#Generate random graph
g <- igraph::erdos.renyi.game(100, 0.1)
igraph::E(g)$weight <- rexp(length(igraph::E(g)), rate=10) #random edge weights from exp(10)
E_List <- cbind(igraph::as_edgelist(g), igraph::E(g)$weight)
colnames(E_List) <- c("n1", "n2", "weight")
sparse_dist <- simplifyNet::irefit(E_List, func=mean.weight.degree, tol = 0.1)
```

lans

Local Adaptive Network Sparsification

Description

Remove all edges under certain probability of the fractional edge weight, alpha.

Usage

```
lans(network, alpha, output, directed = FALSE)
```


Arguments

network	Weighted adjacency matrix, weighted igraph network, or edge list formatted n1 n2 weight with colnames c("n1", "n2", "weight").
alpha	The alpha value is a predetermined threshold to designate statistically important edges by their fractional edge weight at each node. If the probability of choosing that edge via the CDF is less than or equal to alpha, then the edge is not included.
output	If the output should be directed or undirected. Default is that the output is the same as the input based on adjacency matrix symmetry. If the default is overridden, set as either "undirected" or "directed".
directed	If TRUE, specifies that the inputted network is directed. Default is FALSE.

Details

For more information on finding alpha values, see: <https://journals.plos.org/plosone/article?id=10.1371/journal.pone.0016431>

Value

Weighted adjacency matrix of sparsified network.

Author(s)

Andrew Kramer
Alexander Mercier

References

Foti, N. J., Hughes, J. M., & Rockmore, D. N. (2011). Nonparametric sparsification of complex multiscale networks. *PloS one*, 6(2), e16431.

Examples

```
#Generate random ER graph with uniformly random edge weights
g = igraph::erdos.renyi.game(100, 0.1)
igraph::E(g)$weight <- runif(length(igraph::E(g)))
#Sparsify g via LANS
S = lans(g, alpha = 0.3, output = "undirected", directed = FALSE)
#Convert sparsifier to edge list
S_List = simplifyNet::Mtrx_EList(S, directed = FALSE)
sg = simplifyNet::net.as(S_List, net.to="igraph", directed=FALSE)
igraph::ecount(sg)/igraph::ecount(g)#fraction of edges in the sparsifier
```

Mtrx_EList	<i>Adjacency matrix to edge list</i>
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Description

Convert an adjacency matrix to an edge list.

Usage

```
Mtrx_EList(A, directed = FALSE)
```

Arguments

A	Weighted adjacency matrix.
directed	Specifies if the network is directed or undirected. Default is set to undirected.

Value

An edge list, E_List, of adjacency matrix, A, of the form | n1 | n2 | weight |.

Author(s)

Alexander Mercier

net.as	<i>Network format converter</i>
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Description

Convert a network in weighted adjacency matrix, edge list, or igraph to a weighted adjacency matrix, edge list, or igraph format.

Usage

```
net.as(network, net.to = "E_List", directed = FALSE)
```

Arguments

network	Weighted adjacency matrix, weighted igraph network, or edge list formatted n1 n2 weight with colnames c("n1", "n2", "weight").
net.to	Specifies to what format the imputed network is to be converted: (1) 'E_List' convert to an edge list of the format n1 n2 weight with colnames c("n1", "n2", "weight"). (2) 'Adj' convert to a weighted adjacency matrix. (3) 'igraph' convert to a weighted igraph object.
directed	If TRUE, specifies that the inputted network is directed. Default is FALSE.

net.as

11

Value

A network of the format specified by `net . to`.

Author(s)

Alexander Mercier

Index

bestpath, [2](#)

EffR, [3](#)

EffRSparse, [4](#)

EList_Mtrx, [6](#)

gns, [6](#)

irefit, [7](#)

lans, [8](#)

Mtrx_EList, [10](#)

net.as, [10](#)